

OSNOVI ELEKTRONIKE  
Modul elektroenergetika (3OEP3A01, 2OEP3O03)

**1. Zadatak**

Parametri tranzistora u kolu na slici su:

$V_{BE} = 0,7 \text{ V}$ ;  $\beta = 80$ ;  $V_A = 50 \text{ V}$ . Elementi

kola su:

$R_B = 540 \text{ k}\Omega$ ,  $R_C = 4 \text{ k}\Omega$ ,  $R_E = 1,5 \text{ k}\Omega$ ,

$R_g = 2 \text{ k}\Omega$ ,  $R_p = 6 \text{ k}\Omega$ ,  $V_{CC} = 9 \text{ V}$ ,  $C_S \rightarrow \infty$ .

Određiti:

a) Radnu tačku tranzistora ( $V_{CE}$ ,  $I_C$ );

b) Parametre naizmeničnog režima

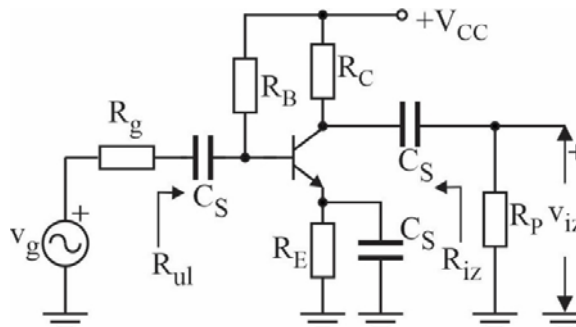
rada ( $r_\pi$ ,  $r_o$ ,  $g_m$ );

c) Naponsko

pojačanje

$$A = \frac{v_O}{v_g}$$

d) Izlaznu otpornost  $R_{iz}$



Rešenje:

a)

$$V_{CC} - R_B \cdot I_B - V_{BE} - R_E \cdot (1 + \beta) \cdot I_B = 0$$

$$I_B = \frac{V_{CC} - V_{BE}}{R_B + R_E \cdot (1 + \beta)} = 12,5 \mu\text{A}$$

$$I_C = \beta I_B = 1 \text{ mA}$$

$$V_C = V_{CC} - R_C(I_C + I_B)$$

$$V_E = R_E I_E$$

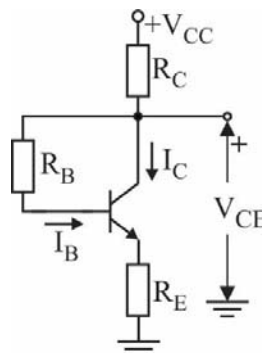
$$V_{CE} = V_{CC} - R_C(I_C + I_B) - R_E I_E = 3,43 \text{ V}$$

b)

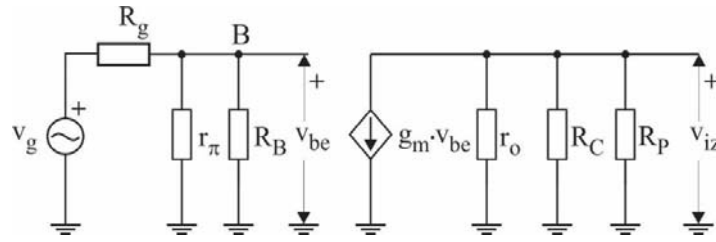
$$r_\pi = \frac{V_T}{I_B} = \frac{26 \text{ mV}}{12,5 \mu\text{A}} = 2,08 \text{ k}\Omega$$

$$g_m = \frac{h_{21E}}{r_\pi} = \frac{I_C}{V_T} = 38,46 \text{ mS}$$

$$r_o = \frac{V_A}{I_C} = \frac{50 \text{ V}}{1 \text{ mA}} = 50 \text{ k}\Omega$$



b)



$$(B) \quad \frac{v_b}{R_B} + \frac{v_b}{r_\pi} + \frac{v_b - v_g}{R_g} = 0$$

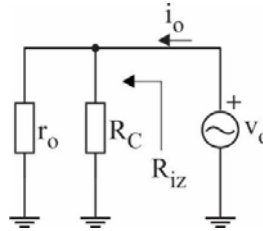
$$g_m v_{be} + \frac{v_{iz}}{r_o} + \frac{v_{iz}}{R_C} + \frac{v_{iz}}{R_P} = 0$$

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$$A = \frac{v_{iz}}{v_g} = -g_m (r_o \parallel R_C \parallel R_P) \frac{r_\pi R_B}{R_g r_\pi + R_B R_g + r_\pi R_B} = 44$$

c)

$$R_{iz} = \frac{v_o}{i_o} = R_C \parallel r_o = 3,7 \text{ k}\Omega$$



## 2. Zadatak

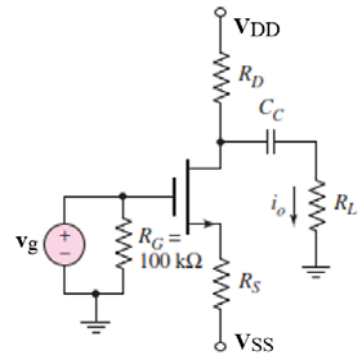
Parametri tranzistora u kolu sa slike su  $A = 0,5 \text{ mA/V}^2$ ,  $V_t = 2,5 \text{ V}$ ,  $\lambda = 0,01 \text{ V}^{-1}$ . Elementi kola su  $R_S = 250 \Omega$ ,  $R_D = 2 \text{ k}\Omega$ ;  $R_L = 2 \text{ k}\Omega$ ,

$V_{DD} = 5 \text{ V}$ ,  $V_{SS} = -5 \text{ V}$ . Odrediti:

a) Radnu tačku tranzistora i dinamičke parametre tranzistora.

b) Naponsko pojačanje  $A_n = v_{iz}/v_g$ .

c) Izlaznu otpornost tranzistora  $R_{iz}$ .



Rešenje:

$$V_S = R_S \cdot I_D + V_{SS}$$

$$V_{GS} = -V_S = -V_{SS} - R_S \cdot I_D$$

$$I_D = A \cdot (V_{GS} - V_t)^2$$

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$$V_{GS} - V_t + V_t = -R_S \cdot A \cdot (V_{GS} - V_t)^2 - V_{SS}$$

$$R_S \cdot A \cdot V_x^2 + V_x + V_{SS} + V_t = 0$$

$$0,125 \cdot V_x^2 + V_x - 2,5 = 0$$

$$V_x = \frac{-1 \pm \sqrt{1 + 4 \cdot 2,5 \cdot 0,125}}{0,25}$$

~~$$V_{x1} = -10 V$$~~

$$V_{x2} = 2 V$$

$$I_D = A \cdot V_x^2 = 2 mA$$

$$g_m = 2 \cdot \sqrt{A \cdot I_D} = 2 mS$$

$$r_o = \frac{1}{\lambda \cdot I_D} = 50 k\Omega$$

$$\mu = r_o \cdot g_m = 100$$

b)

$$R_D \parallel R_L \cdot i_d + r_o \cdot i_d - \mu \cdot v_{gs} + R_S \cdot i_d = 0$$

$$v_{gs} = v_g - i_d \cdot R_S$$

$$v_{iz} = -R_D \parallel R_L \cdot i_d$$

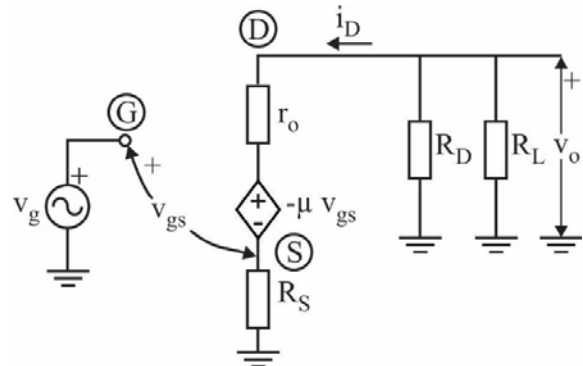
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$$R_D \parallel R_L \cdot i_d + r_o \cdot i_d - \mu \cdot v_g + \mu \cdot i_d \cdot R_S + R_S \cdot i_d = 0$$

$$i_d = \frac{\mu \cdot v_g}{R_D \parallel R_L + r_o + (\mu + 1) \cdot R_S}$$

$$v_{iz} = \frac{-R_D \parallel R_L \cdot \mu \cdot v_g}{R_D \parallel R_L + r_o + (\mu + 1) \cdot R_S}$$

$$A_n = \frac{v_{iz}}{v_g} = -\frac{R_D \parallel R_L \cdot \mu}{R_D \parallel R_L + r_o + (\mu + 1) \cdot R_S} = -13,1$$



c)

$$r_o \cdot i_d - \mu \cdot v_{gs} + R_S \cdot i_d = v_o$$

$$v_{gs} = -i_d \cdot R_S$$

$$i_o = i_d + \frac{v_o}{R_D \parallel R_L}$$

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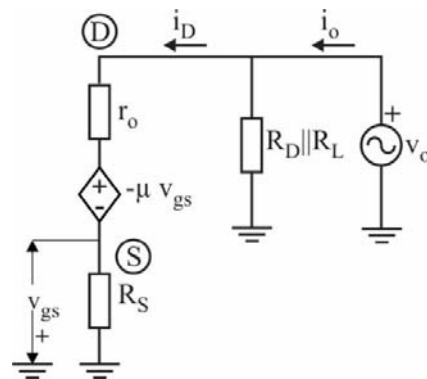

$$i_d = \frac{v_o}{r_o + (\mu + 1) \cdot R_S}$$

$$R_{izt} = \frac{v_o}{i_d}$$

$$R_{izt} = r_o + (\mu + 1) \cdot R_S = 75 k\Omega$$

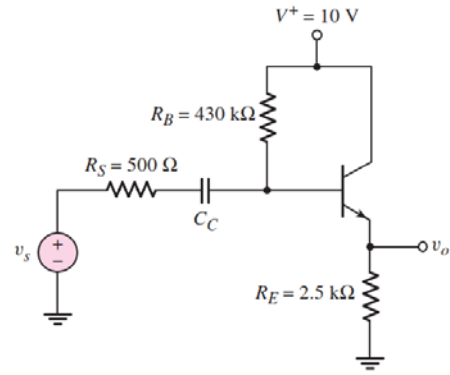
$$i_o = \frac{v_o}{R_{izt}} + \frac{v_o}{R_D \parallel R_L}$$

$$R_{iz} = \frac{v_o}{i_o} = \frac{1}{\frac{1}{R_{izt}} + \frac{1}{R_D \parallel R_L}} = R_{izt} \parallel R_D \parallel R_L = 0,98 k\Omega$$



### 3. Zadatak

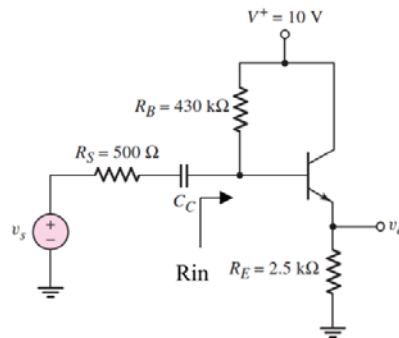
Kolo na slici je izlazni stepen audio pojačavača. Parametri tranzistora su:  $V_{BE}=0,6\text{ V}$ ;  $h_{21E}=b=200$ ;  $h_{22E}=0\text{ S}$ . Odrediti kapacitivnost kondenzatora  $C_C$  tako da donja granična frekvencija ovog kola iznosi 15 Hz.



### Rešenje:

Da bi odredili otpornost koja se vidi sa krajeva kondenzatora potrebno je odrediti ulaznu otpornost  $R_{in}$ .

$$\tau = C_C \cdot (R_S + R_{in})$$

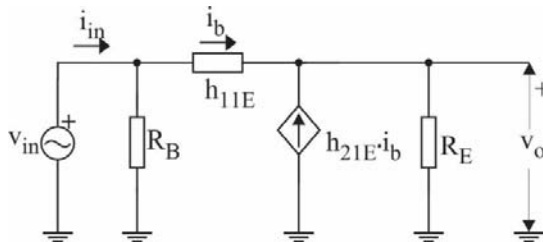
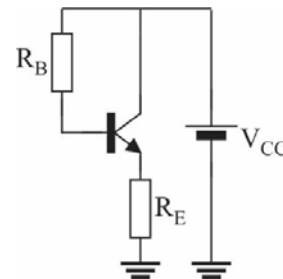


$$-V_{CC} + R_B \cdot I_B + V_{BE} + R_E \cdot I_E = 0$$

$$I_B = \frac{V_{CC} - V_{BE}}{R_B + R_E \cdot (1 + \beta)} = 11,3 \mu\text{A}$$

$$h_{11E} = r_\pi = \frac{V_T}{I_B} = \frac{26\text{ mV}}{11,3 \mu\text{A}} = 2,3\text{ k}\Omega$$

$$h_{21E} = \beta$$



$$-i_{in} + \frac{v_{in}}{R_B} + i_b = 0$$

$$-i_b - h_{21E} \cdot i_b + \frac{v_o}{R_E} = 0$$

$$i_b = \frac{v_{in} - v_o}{h_{11E}}$$

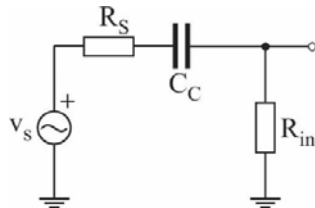
$$i_b \cdot h_{11E} = v_{in} - R_E \cdot (1 + h_{21E}) \cdot i_b$$

$$i_b = \frac{v_{in}}{h_{11E} + R_E \cdot (1 + h_{21E})}$$

$$R_t = \frac{v_{in}}{i_b} = h_{11E} + R_E \cdot (1 + h_{21E}) = 504,8 \text{ k}\Omega$$

$$i_{in} = \frac{v_{in}}{R_t} + \frac{v_{in}}{R_B}$$

$$R_{in} = R_B \parallel R_t = 232 \text{ k}\Omega$$



$$\tau = C_C \cdot (R_S + R_{in})$$

$$\omega_d = \frac{1}{\tau} = \frac{1}{C_C \cdot (R_S + R_{in})}$$

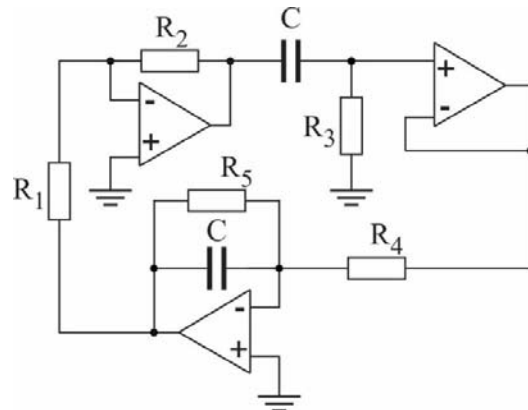
$$C_C = \frac{1}{\omega_d \cdot (R_S + R_{in})} = \frac{1}{6,28 \cdot 15 \cdot (2,32 \cdot 10^5 + 500)} \text{ F} = 46 \text{ nF}$$

#### 4. Zadatak

Za oscilator prostoperiodičnih oscilacija prikazan na slici odrediti:

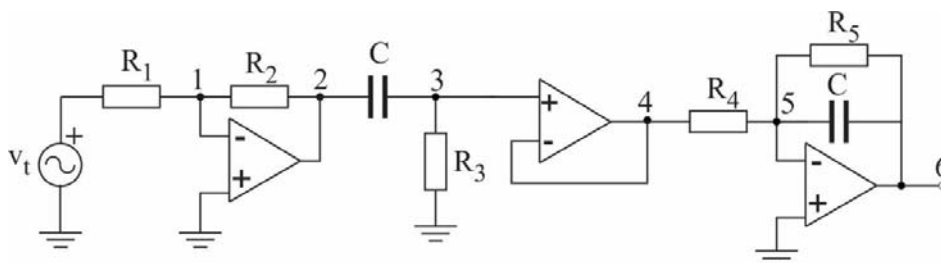
- Analitički izraz kružnog pojačanja;
- Vrednost otpornika  $R_4$  pri kojoj je ispunjen uslov oscilovanja;
- Frekvenciju oscilovanja.

Poznato je:  $R_1 = 1 \text{ k}\Omega$ ,  $R_2 = 4 \text{ k}\Omega$ ,  $R_3 = 5 \text{ k}\Omega$ ,  $R_5 = 5 \text{ k}\Omega$ ,  $C = 1 \text{ nF}$ . Operacioni pojačavači su idealni.



Slika 4

Rešenje:



$$V_1 \cdot \left( \frac{1}{R_1} + \frac{1}{R_2} \right) - V_t \frac{1}{R_1} - V_2 \frac{1}{R_2} = 0$$

$$V_3 \cdot \left( \frac{1}{R_3} + s \cdot C \right) - V_2 \cdot sC = 0$$

$$V_5 \cdot \left( \frac{1}{R_4} + \frac{1}{R_5} + sC \right) - V_4 \cdot \frac{1}{R_4} - V_6 \cdot \left( sC + \frac{1}{R_5} \right) = 0$$

$$V_1 = 0$$

$$V_3 = V_4$$

$$V_5 = 0$$


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$$AB = \frac{V_6}{V_t} = \frac{V_6}{V_4} \cdot \frac{V_4}{V_2} \cdot \frac{V_2}{V_t} = 1 + j \cdot 0$$

$$AB = \frac{V_6}{V_t} = \left( -\frac{R_5}{R_4 + sCR_5R_4} \right) \cdot \frac{sCR_3}{sCR_3 + 1} \cdot \left( -\frac{R_2}{R_1} \right)$$

$$AB = \frac{SCR_2R_3R_5}{R_1R_4 + sCR_1R_4(R_3 + R_5) + s^2 C^2R_1R_3R_4R_5}$$

Iz uslova  $AB=1+j \cdot 0$  sledi:

$$R_1R_4 + sCR_1R_4(R_3 + R_5) + s^2 C^2R_1R_3R_4R_5 = SCR_2R_3R_5$$

$$R_1R_4 + j\omega CR_1R_4(R_3 + R_5) - j\omega CR_2R_3R_5 - \omega^2 C^2R_1R_3R_4R_5 = 0$$

b)

Kada se izdvoje imaginarni deo jednacine dobija se:

$$j\omega CR_1R_4(R_3 + R_5) - j\omega CR_2R_3R_5 = 0$$

$$R_1R_4(R_3 + R_5) - R_2R_3R_5 = 0$$

$$R_4 = \frac{R_3R_5}{R_3 + R_5} \cdot \frac{R_2}{R_1} = 10 \text{ k}\Omega$$

c)

Izdvajanjem realnih sabiraka jednacine dobija se:

$$R_1R_4 - \omega^2 C^2R_1R_3R_4R_5 = 1$$

$$\omega_0 = \frac{1}{C\sqrt{R_3R_5}} = 2 \cdot 10^5 \frac{\text{rad}}{\text{s}}$$

$$f_0 = \frac{\omega_0}{2\pi} = 31,8 \text{ kHz}$$