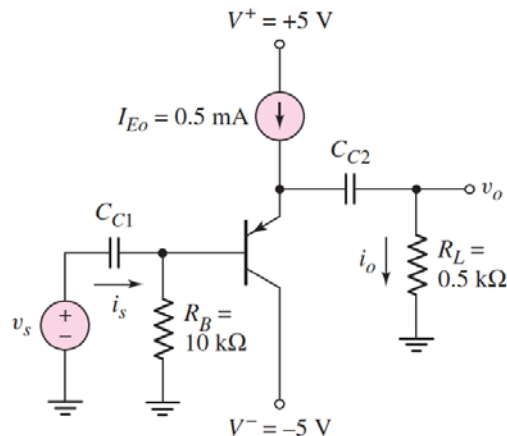


**OSNOVI ELEKTRONIKE**  
**Modul elektroenergetika (3OEP3A01, 2OEP3O03)**

**1. Zadatak**

Na slici 1 prikazan je pojačavač u sprezi sa zajedničkom bazom. Polarizacija kola je realizovana jednosmernim strujnim generatorom  $I_{Eo} = 0,5 \text{ mA}$ . Poznato je:  $\beta = 80$ ,  $V_{BE} = 0,7 \text{ V}$ ;  $C_{c1} \rightarrow \infty$ ,  $R_B = 10 \text{ k}\Omega$ ;  $R_L = 500 \Omega$ . U tačkama  $a, b$  i  $c$  smatrati da  $C_{c2} \rightarrow \infty$ . Odrediti:



Slika 1

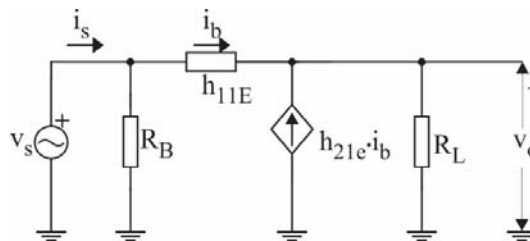
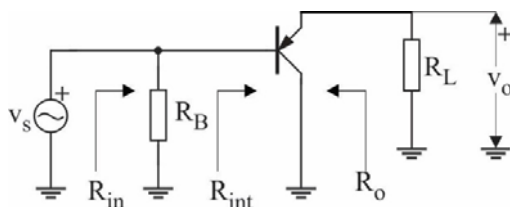
- Ulaznu otpornost  $R_{in} = \frac{v_s}{i_s}$
- Naponsko pojačanje  $A = \frac{v_o}{v_s}$
- Izlaznu otpornost  $R_o$ ;
- Donju graničnu frekvenciju pojačavača ukoliko je  $C_2 = 0,1 \mu\text{F}$

Rešenje

a)

$$I_B = \frac{I_{Eo}}{1 + \beta} = 6,17 \mu\text{A}$$

$$h_{11E} = \frac{V_T}{I_B} = \frac{26 \text{ mV}}{6,17 \mu\text{V}} = 4,2 \text{ k}\Omega$$



$$-i_b - h_{21E} \cdot i_b + \frac{v_o}{R_L} = 0$$

$$i_b = \frac{v_s - v_o}{h_{11E}}$$

$$v_o = i_b \cdot R_L + h_{21E} \cdot i_b \cdot R_L$$

$$v_s = h_{11E} \cdot i_b + v_o$$

$$v_s = h_{11E} \cdot i_b + i_b \cdot R_L + h_{21E} \cdot i_b \cdot R_L$$

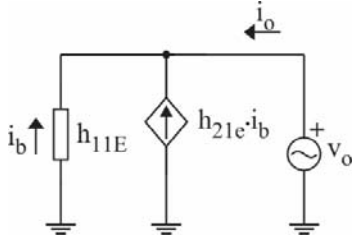
$$R_{int} = \frac{v_s}{i_b} = h_{11E} + R_L + h_{21E} \cdot R_L = 44,7 \text{ k}\Omega$$

$$R_{in} = R_{int} \parallel R_B = 8,17 \text{ k}\Omega$$

b)

$$A_n = \frac{v_o}{v_s} = \frac{i_b}{v_s} \cdot \frac{v_o}{i_b} = \frac{1}{R_{int}} \cdot (1 + h_{21E}) \cdot R_L = \frac{(1 + h_{21E}) \cdot R_L}{h_{11} + R_L + h_{21E} \cdot R_L} = 0,9$$

c)



$$i_b = -\frac{v_o}{h_{11E}}$$

$$-i_o - i_b - h_{21E} \cdot i_b = 0$$

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$$i_o = v_o \cdot \left( \frac{1 + h_{21E}}{h_{11E}} \right)$$

$$R_o = \frac{v_o}{i_o} = \frac{h_{11E}}{(1 + h_{21E})} = 52 \Omega$$

d)

$$\tau = C_{C2} \cdot (R_o + R_L)$$

$$\omega_d = \frac{1}{\tau} = \frac{1}{C_{C2}(R_o + R_L)} = 1,81 \cdot 10^4 \frac{rad}{s}$$

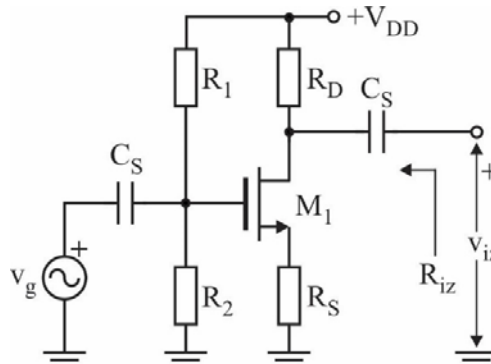
$$f_d = \frac{\omega_d}{2\pi} = 2.89 \text{ kHz}$$

## 2. Zadatak

Za kolo pojačavača sa slike odrediti:

- Dinamičke parametre tranzistora: strminu  $g_m$ , izlaznu otpornost  $r_o$  i koeficijent naponskog pojačanja  $\mu$  ako je  $\lambda = 0,01 \text{ V}^{-1}$ ;
- Naponsko pojačanje  $A_n = v_{iz}/v_g$ .
- Izlaznu otpornost tranzistora  $R_{iz}$ ;

Poznato je  $R_S = 1 \text{ k}\Omega$ ,  $R_D = 6 \text{ k}\Omega$ ,  $R_1 = 3 \text{ M}\Omega$ ,  $R_2 = 1 \text{ M}\Omega$  i  $V_{DD} = 12 \text{ V}$ .  $C_S$  teži beskonačnosti. Parametri tranzistora su:  $A = 1 \text{ mA/V}^2$  i  $V_t = 1 \text{ V}$ .



Rešenje

a)

$$V_G = \frac{R_2}{R_1 + R_2} \cdot V_{DD}$$

$$V_S = R_S \cdot I_D$$

$$I_D = A \cdot (V_{GS} - V_t)^2$$

$$V_x = V_{GS} - V_t$$

$$V_{GS} = \frac{R_2}{R_1 + R_2} \cdot V_{DD} - R_S \cdot A \cdot (V_{GS} - V_t)^2$$

$$R_S \cdot A \cdot (V_{GS} - V_t)^2 + (V_{GS} - V_t) + V_t - \frac{R_2}{R_1 + R_2} \cdot V_{DD} = 0$$

$$R_S \cdot A \cdot V_x^2 + V_x + V_t - \frac{R_2}{R_1 + R_2} \cdot V_{DD} = 0$$

$$V_x^2 + V_x - 2 = 0$$

$$V_x = \frac{-1 \pm \sqrt{1 + 8}}{2}$$

$$V_{x1} = 1 \text{ V}$$

$$V_{x2} = -2 \text{ V}$$

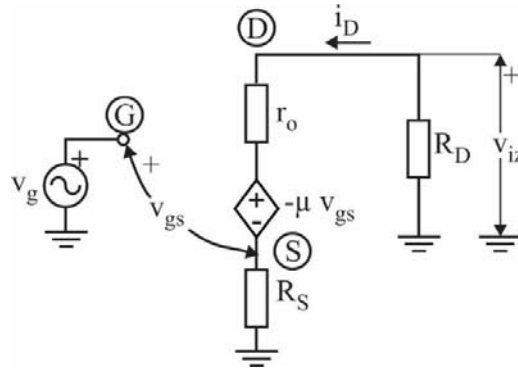
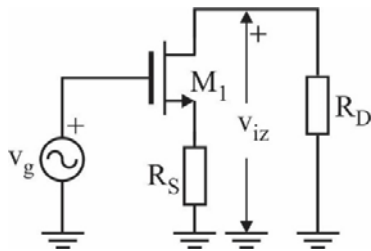
$$I_D = A \cdot V_x^2 = 1 \text{ mA}$$

$$g_m = 2 \cdot \sqrt{A \cdot I_D} = 2 \text{ mS}$$

$$r_o = \frac{1}{\lambda \cdot I_D} = 100 \text{ k}\Omega$$

$$\mu = g_m \cdot r_o = 200$$

b) Otpornici R1 i R2 su izostavljeni iz šeme jer ne uticu na naponsko pojačanje. Ova dva otpornika imaju uticaj samo na ulaznu otpornost.



$$R_D \cdot i_d + r_o \cdot i_d - \mu \cdot v_{gs} + R_S \cdot i_d = 0$$

$$v_{gs} = v_g - i_d \cdot R_S$$

$$v_{iz} = -R_D \cdot i_d$$

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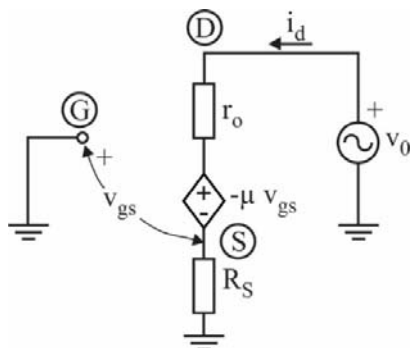
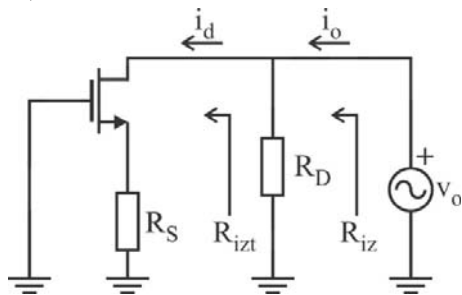

$$R_D \cdot i_d + r_o \cdot i_d - \mu \cdot v_g + \mu \cdot i_d \cdot R_S + R_S \cdot i_d = 0$$

$$i_d = \frac{\mu \cdot v_g}{R_D + r_o + (\mu + 1) \cdot R_S}$$

$$v_{iz} = \frac{-R_D \cdot \mu \cdot v_g}{R_D + r_o + (\mu + 1) \cdot R_S}$$

$$A_n = \frac{v_{iz}}{v_g} = \frac{-R_D \cdot \mu}{R_D + r_o + (\mu + 1) \cdot R_S} = -3,9$$

c)



$$v_o = r_o \cdot i_d - \mu \cdot v_{gs} + R_s \cdot i_d$$

$$v_{gs} = -R_s \cdot i_d$$

$$v_o = r_o \cdot i_d + \mu \cdot R_s \cdot i_d + R_s \cdot i_d$$

$$R_{izt} = \frac{v_o}{i_d} = r_o + (\mu + 1) \cdot R_s = 301 \text{ k}\Omega$$

$$R_{iz} = R_{izt} \parallel R_D = 5,88 \text{ k}\Omega$$

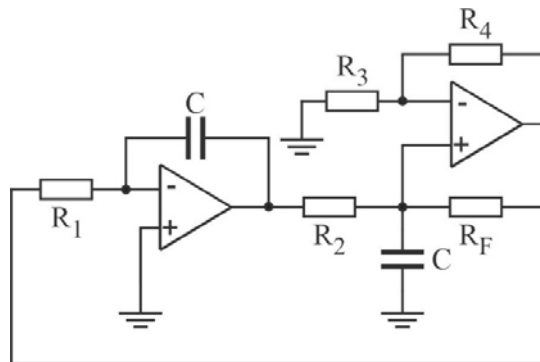
$$R_{iz} \approx R_D$$

### 3. Zadatak

Za oscilator prostoperiodičnih oscilacija prikazan na slici odrediti:

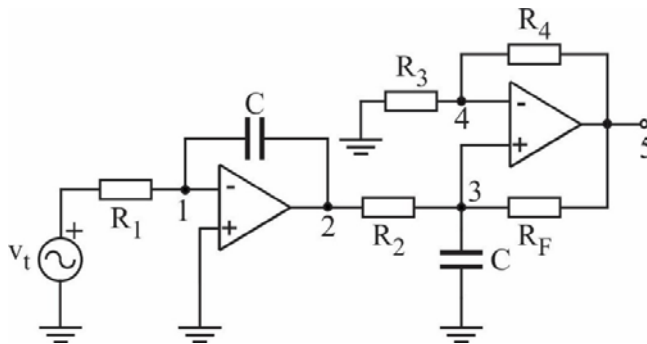
- Analitički izraz kružnog pojačanja;
- Vrednost otpornika  $R_F$  pri kojoj je ispunjen uslov oscilovanja;
- Frekvenciju oscilovanja.

Poznato je:  $R_1 = 2 \text{ k}\Omega$ ,  $R_2 = 1 \text{ k}\Omega$ ,  $R_3 = R_4 = 5 \text{ k}\Omega$ ,  $C = 10 \text{ nF}$ . Operacioni pojačavači su idealni.



Rešenje

a)



$$V_1 \cdot \left( \frac{1}{R_1} + sC \right) - V_t \frac{1}{R_1} - V_2 sC = 0$$

$$V_3 \cdot \left( \frac{1}{R_2} + \frac{1}{R_F} + s \cdot C \right) - V_2 \cdot \frac{1}{R_2} - V_5 \cdot \frac{1}{R_F} = 0$$

$$V_4 \cdot \left( \frac{1}{R_3} + \frac{1}{R_4} \right) - V_5 \cdot \frac{1}{R_4} = 0$$

$$V_1 = 0$$

$$V_3 = V_4$$

$$AB = \frac{V_5}{V_t} = \frac{V_2}{V_t} \cdot \frac{V_5}{V_2} = \left( -\frac{1}{sCR_1} \right) \cdot \frac{R_F(R_4 + R_3)}{R_F R_3 - R_2 R_4 + sCR_2 R_3 R_F}$$

Iz uslova  $AB=1+j0$  sledi:

$$sCR_1 R_3 R_F - sCR_1 R_2 R_4 + s^2 C^2 R_1 R_2 R_3 R_F = -R_F R_4 - R_F R_3$$

$$-\omega^2 C^2 R_1 R_2 R_3 R_F + j\omega CR_1 R_3 R_F - j\omega CR_1 R_2 R_4 + R_F R_4 + R_F R_3 = 0$$

b)

Kada se izdvoje imaginarni deo jednačine dobija se:

$$j\omega CR_1 R_3 R_F - j\omega CR_1 R_2 R_4 = 0$$

$$R_3 R_F - R_2 R_4 = 0$$

$$R_4 = \frac{R_2 R_4}{R_3} = 1 \text{ k}\Omega$$

c)

Izdvajanjem realnih sabiraka jednačine dobija se:

$$-\omega^2 C^2 R_1 R_2 R_3 R_F + R_F R_4 + R_F R_3 = 0$$

Frekvencija oscilovanja je:

$$\omega_0 = \sqrt{\frac{R_3 + R_4}{C^2 R_1 R_2 R_3}} = 10^5 \frac{\text{rad}}{\text{s}}$$

$$f_0 = \frac{\omega_0}{2\pi} = 15,9 \text{ kHz}$$